

Multiplication & Division Calculation Policy

Highlands Primary School

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#### EYFS:

Children will learn to solve problems, including doubling, halving and sharing.

EYFS end of year expectations	Concrete	Pictorial	Abstract	Using and applying
Solves problems, including doubling, halving and sharing (ELG). (Numbers)	Using objects to show double. Using objects to show half and to share.	Drawing pictures to show double and to half or 'share'.		If Megan has 3 toys and Maheen has 3 toys, how many toys do they have altogether?

Key Stage 1:

- The principal focus of mathematics teaching in key stage 1 is to ensure that pupils develop confidence and mental fluency with whole numbers, counting and place value. This should involve working with numerals, words and the four operations, including with practical resources (for example, concrete objects and measuring tools).
- By the end of year 2, pupils should know the number bonds to 20 and be precise in using and understanding place value. An emphasis on practice at this early stage will aid fluency.

End of year expectations	Rapid recall	Mental calculation	Language	Using and applying
Year 1		Count on and back in 2, 5	Groups of	Solve simple one-step problems that involve using
		and 10.	Array	concrete objects and pictorial representations.
			Counting in	
			Sharing	
			Double	
			Half	
			Quarter	
Year 2	Identifying odd and even	Count in steps of 3 from 0	Odd, even,	Solve one-step problems involving multiplication
	numbers.	and in tens from any	Repeated	and division, using materials, arrays, repeated
	Recall multiples of 2, 5 and	number, forward or	addition/subtraction	addition, mental methods, and multiplication and
	10 and related division facts.	backward.	Grouping/ sharing	division facts, including problems in contexts.
			Inverse	
			Multiply Multiple(s) of	They connect the 10 multiplication table to place
			Divide	value, and the 5 multiplication table to the
			Division	divisions on the clock face.
			Commutative	
			Calculate	
			Equivalent	

Year 1	Concrete	Pictorial	Conceptual	Using & applying
Multiplication and division as repeated addition and subtraction	Using familiar objects and resources. Finding 'groups of' with repeated addition and subtraction.	Repeated images E.g. How many legs?	2+2+2 5+5+5+5	Making links If one teddy has two apples, how many apples will three teddies have?
Represent repeated addition as an array. Begin to use arrays to find repeated subtraction.	Make arrays on grids with counting objects	Understand visual representations of arrays	2+2+2 5+5+5+5 12-3-3-3-3=0	Here are 10 lego people If 2 people fit into the train carriage, how many carriages do we need? Practical If we put two pencils in each pencil pot how many pencils will we need?
Doubling and halving numbers within 20 (as repeated addition and subtraction).	Using familiar objects and resources.	Using a variety of models and images.	Using number sentences and beginning to calculate mentally. 6 + 6 = Double 9 = 14 = Double Half of 18 = $\frac{1}{2}$ of $\Box = 5$ 10 = half of $7 = 14 - \Box$ $4 + \Box = 8$	Class 1 has 8 girls. Class 2 has <b>double</b> the number of girls. How many girls are there in Class 2?

Year 2	Concrete	Pictorial	Conceptual	Using and applying
Use arrays to make or draw multiplications and find the corresponding division facts. Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (×), division (÷) and equals (=) sign	Make arrays on grids using counting objects.     Identify arrays in everyday objects.	Array images Array images Repeated addition and subtraction along a number line. $ \underbrace{+3}_{0} \underbrace{+3}_{-5} \underbrace$	Using number sentences and beginning to calculate mentally. $3 \times 4 = 12$ $12 \div 4 = 3$ Missing number problems. $20 = \Box \times 5$ $3 = \Box \div 6$	I had 20 lollies. I put them into <b>groups</b> of 5. How many groups were there? I had 20 lollies. I <b>shared</b> them between 5 people. How many lollies did each person get? I saved 5p <b>each</b> week for 6 weeks. How much did I save altogether? If I save 5p <b>each</b> week, how many weeks will it take me to save 40p?
Show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot.	Make arrays on grids using counting objects. $2 \times 4 = 8$ Rotating arrays to find other multiplications. $4 \times 2 = 8$	Repeated addition and subtraction along a number line. -5 $-5$ $-50$ $5$ $10$ $153 \times 5 = 15-3 \times 5 = 15-3 \times 3 = 15$	Using number sentences and beginning to calculate mentally. $3 \times 5 = 15$ $5 \times 3 = 15$ $15 \div 5 = 3$ $15 \div 3 = 5$	There are 24 parents coming to watch our class assembly. How many different ways can you arrange the chairs? (In equal rows).

#### Lower Key Stage 2:

- The principal focus of mathematics teaching in lower key stage 2 is to ensure that pupils become increasingly fluent with whole numbers and the four operations, including number facts and the concept of place value. This should ensure that pupils develop efficient written and mental methods and perform calculations accurately with increasingly large whole numbers.
- At this stage, pupils should develop their ability to solve a range of problems, including with simple fractions and decimal place value. By the end of year 4, pupils should have memorised their multiplication tables up to and including the 12 multiplication table and show precision and fluency in their work.

End of year expectations	Rapid recall	Mental calculation	Language	Using and applying
Year 3	Recall multiples of 2, 5 and 10 and related division facts. Begin to recall multiples of 3, 6 and 4 and 8 and related division facts.	Count from 0 in multiples of 4, 8, 50 and 100.	Grid method Product Short division Remainder	Pupils should solve simple problems in contexts, including missing number problems, deciding which of the four operations to use and why, including measuring and scaling contexts, and correspondence problems in which m objects are connected to n objects (e.g. 3 hats and 4 coats, how many different outfits; 12 sweets shared equally between 4 children; 4 cakes shared equally between 8 children).
Year 4	Recall multiplication and division facts for multiplication tables up to 12 × 12	Count in multiples of 6, 7, 9, 25 and 1000 Multiply 3 numbers U x U x U Recall factor pairs for a given number Multiply by 0 and 1 and divide by 1	Factor Factor pair Quotient Divisor	Pupils should solve <b>two-step</b> problems in contexts, choosing the appropriate operation, working with increasingly harder numbers. This should include correspondence questions such as three cakes shared equally between 10 children.

Year 3	Concrete	Pictorial	Conceptual	Using & applying
Year 3 TU x U Extending understanding of arrays (TU x U), progressing to formal written methods	Using counting objects and resources. 23 x 4 = 92 Ten s Units	Use arrays to link to grid multiplications. Tens Units X 20 3 4 80 12 80 + 12 = 92 Children can also write the expanded calculations within the grid e.g. 4x20=80 and	ConceptualUsing number sentences. $18 \ge 4 = \square$ $31 \ge 3 = \square$ Missing number problems. $\square \ge 41 = 123$ $7 \ge 84$	Using & applyingYear 3 went on a trip. Therewere 6 groups with 14children in each group. Howmany children went on thetrip in total?Use the digits 2, 3, 4, 5 and 6.Make a multiplication (U xTU) e.g. 2 x 53 =Find different totals can youfind?How many multiplicationshave the same total?
	Begin to link to inverse operations: $92 \div 4 = 23$	the grid e.g. 4x20=80 and 4x3=12.		

Year 3	Concrete	Pictorial	Conceptual	Using & applying
TU ÷ U Sharing and grouping to create an array. ( <i>Not</i> exchanging from tens to units at this stage).	Using counting objects and resources. $69 \div 3 = 23$ 10 $10$ $1$ $1$ $110$ $10$ $1$ $1$ $110$ $10$ $1$ $1$ $110$ $10$ $1$ $1$ $110$ $10$ $1$ $1$ $110$ $10$ $1$ $1$ $110$ $10$ $1$ $1$ $110$ $10$ $1$ $1$ $1Check using multiplication inverse:23 \times 3 = 69$	Repeated subtraction on a number line. $ \underbrace{\begin{array}{c} & -4 & -4 & -4 & -4 \\ \hline 0 & 3 & 7 & 11 & 15 & 19 & 23 \\ \hline \end{array}} $ Extending divisions to resemble written method of short division. 23 3 3 69 ÷ 3 = 23	Short division. $ \begin{array}{c} 23\\ 3\overline{69}\\ \end{array} $ Check using multiplication inverse: $ \begin{array}{c c} x & 20 & 3\\ \hline 3 & 60 & 9\\ \hline 60 + 9 = 69\\ \end{array} $	<ul> <li>69 children were grouped equally onto 3 buses for a trip. How many children went on each bus?</li> <li>3 children shared £69 equally. How much did they each receive?</li> <li>How many different divisions can you make?</li> <li>36 ÷ ? = ?</li> </ul>
Understand the concept of remainders after division.	Using resources. 23 ÷ 4 = 5 r3	Repeated addition and subtraction along a number line. 23 ÷ 4 = 5 r3 $\underbrace{\overset{+4}{0} \overset{+4}{4} \overset{+4}{8} \overset{+4}{12} \overset{+4}{16} \overset{+4}{20} \overset{-23}{23}}_{0 3 7 11 15 19 23}$	Begin to solve mentally. $23 \div 4 = \square$ $31 \div 6 = \square$ Missing number problems. $\square \div 3 = 4^{r1}$ $17 \div \square = 3^{r2}$	A farmer had 33 eggs. He put them into boxes of 6. How many <b>full</b> boxes did he have? How many eggs did he have left over? If he put them into boxes of 12, how many would be left over now? Use each number in the 4x table. Make it with counters then share it into 3 groups. Write the remainder each time. What patterns do you notice?
Year 4	Concrete	Pictorial	Conceptual	Using and applying

HTU x U multiply 2- digit and 3- digit numbers by a 1-digit number using formal written layout	Crossing one boundary. 126 x 3 = Hundreds Tens Units $\bigcirc$ $\bigcirc$ $\bigcirc$ $\bigcirc$ $\bigcirc$ $\bigcirc$ $\bigcirc$ $\bigcirc$ $\bigcirc$ $\bigcirc$	Beginning with grid         multiplication.         x       100       20       6         3       300       60       18         300 + 60 + 18	Expanded method (if children need this) 126 $\underline{x}$ 3 18 (3 x 6) 60 (3 x 20) <u>300 (3 x 100)</u> 378 <i>If children are ready,</i> <i>move onto compact</i> <i>vertical method.</i> 1 2 6 $\underline{x}$ 3 <u>3 7 8</u> 1	In one week, 163 people visited the museum each day. How many people visited in total? My sister and I were raising money for charity. We collected £127 every day for 6 days. We <b>shared</b> the money <b>equally</b> between two different charities. How much money did each charity receive?
	Extending to crossing <i>two</i> boundaries. 247 x 3 = Hundreds Tens Units m m $m$	Beginning with grid multiplication. x     200     40     7       3     600     120     21 $600 + 120 + 21$	Expanded method (if children need this) 247 <u>x 3</u> 21 (3 x 7) 120 (3 x 40) <u>600 (</u> 3 x 200) <u>741</u> <i>If children are ready,</i> <i>move onto compact</i> <i>vertical method.</i> 2 4 7	Use the digits 1, 2, 3 and 5. Make a multiplication U x HTU. How many different products are there? What are the largest and smallest products possible? U x HTU = 820. How many ways can you solve this?

			$\frac{x  3}{\begin{array}{c} 7  4  1 \\ 1  2 \end{array}}$	
Year 4 TU ÷ U (Where exchanging is required) HTU ÷ U (Where exchanging is required)	Concrete         Grouping and sharing using place         value counters.         Exchanging counters which cannot         be grouped.         138 ÷ 6 = 23 r 0         Hundreds       Tens         Units         Image: Concrete transmit in the second secon	Pictorial         Result of grouping/sharing counters during 'concrete' stage.         Chunking on a number line. $138 \div 6 = 23$ Key Facts $1 \times 6 = 6$ $2 \times 6 = 12$ $5 \times 6 = 30$ $10 \times 6 = 60$	Conceptual Short division methods. $0\ 2\ 3$ $6\ 1\ 3\ 8$ $138 \div 6 = 23$ $432 \div 5$ becomes $8\ 6\ r^2$ $5\ 4\ 3\ 2$ Answer: 86 remainder 2	Using and applyingA school ordered 432 pencils.They were put into packs of5. How many packs weremade? How many pencilswere left over?Robbie has 150 stickers. Hekept 12 and shared the restequally between 6 friends.How many stickers did eachof his friends get?436 children need to be putinto teams for sports day.How many different wayscould the children be groupedequally?How many divisions can youmake which have aremainder of 3? Whatpatterns do you notice?Which numbers between 100and 150 have a remainder of1 when they are divided by 2,3, 4, 5, and 6?

#### Upper Key Stage 2:

- The principal focus of mathematics teaching in upper key stage 2 is to ensure that pupils extend their understanding of the number system and place value to include larger integers. This should develop the connections that pupils make between multiplication and division with fractions, decimals, percentages and ratio.
- At this stage, pupils should develop their ability to solve a wider range of problems, including increasingly complex properties of numbers and arithmetic, and problems demanding efficient written and mental methods of calculation. With this foundation in arithmetic, pupils are introduced to the language of algebra as a means for solving a variety of problems.
- By the end of year 6, pupils should be fluent in written methods for all four operations, including long multiplication and division, and in working with fractions, decimals and percentages.

End of year expectations	Rapid recall	Mental calculation	Language	Using and applying
Year 5	Related decimal facts for tables E.g. 6 x 7 = 42 0.6 x 7 = 0.7 x 6 = 4.2÷7= etc.	Count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000. ÷x 10, 100 or 1000 including decimals Recognise all factor pairs of a number and identify common factors of two numbers know and use the vocabulary of prime numbers, prime factors and composite (nonprime) numbers recognise and use square numbers and cube numbers, and the notation for squared ( 2 ) and cubed (3 )	Prime number Composite number Common factors Square / cube numbers	Solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes Solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign. Solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates.

Year 6	Perform mental calculations,	Use their knowledge of the order of operations to carry out
	including with mixed operations	calculations involving the four operations.
	and large numbers	Solve addition and subtraction multi-step. Problems in
		contexts, deciding which operations and methods to use
	E.g. 3 x 700 + 115 =	and why.
		Solve problems involving addition, subtraction,
	Use estimation to check answers	multiplication and division including interpreting
	to calculations and determine, in	remainders appropriately within the context of the
	the context of a problem, levels of	problem.
	accuracy.	
	identify common factors, common	
	multiples and prime numbers	
	use their knowledge of the order	
	of operations to carry out	
	calculations involving the four	
	operations	

Year 5	Concrete	Pictorial	Conceptual	Using and applying
Multiply numbers up to <b>four</b> <b>digits by a</b>	Refer to Year 4 (HTU x U) and extend the process of using place value counters to ThHTU x U	Use grid method HTU x U and extend to ThHTU x U	Refer to Year 4 expanded vertical method (HTU x U) and extend to ThHTU x U	There are 5 kittens, each weighing 1352g. What is their total mass in Kg?
<b>1 or 2-</b> <b>digit</b> number using a formal written method, including <b>long</b> <b>multiplica</b> <b>tion for 2-</b>	(Year 4) Crossing one boundary. 126 x 3 = $\frac{\text{Hundreds}}{100} = \frac{\text{Tens}}{100} = \frac{\text{Units}}{100} = 1000000000000000000000000000000000000$	(Year 4) Beginning with grid multiplication.	126 <u>x 3</u> 18 (3 x 6) 60 (3 x 20) <u>300 (3 x 100)</u> <u>378</u> Short multiplication.	Use the digits 1 to 5. Make a multiplication: ThHTU x U How many products can you make between 5000 and 5500?

digit numbers			$ \begin{array}{r} 2741 \\ x & 6 \\ \underline{16446} \\ 42 \\ \end{array} $ Answer: 2741 x 6= 16446	
TU x TU	NB: Children should proceed to pictorial methods alongside methods used in year 4.	Grid method: $47 \times 36 =$ $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Compact method: $4 7$ $x 3 6$ $2 8 2$ $\mathcal{A}$ $1 4 1 0$ $\frac{2}{1692}$ Answer: 47 x 36 = 1692	I saved £36 every week for a year. At the end of the year, I gave half of it to charity. How much money did I donate? Try this with several numbers: choose a prime number greater than 3, square it and divide the answer by 12. Look at the remainder. What do you notice? Why does this happen?
HTU x TU	Follow processes shown above (TU x TU).	$x$ $300$ $80$ $2$ $x$ $300$ $80$ $2$ $2$ $20 \times 20 \times 80$ $20 \times 2 =$ $0$ $300 =$ $=$ $40$ $3$ $3 \times 3 \times 80 =$ $3 \times 2 =$ $300 =$ $240$ $6$ $900$ $40$ $900$	Compact method: 1 2 4 x = 26 7 4 4 $\frac{2 4 8 0}{3 2 2 4}$ (6 x 124) $\frac{3 2 2 4}{1 1}$ (20 x 124) Answer: 124 x 26 = 3224	There are 24 bottles in a crate. Each bottle has a capacity of 720ml. what is the total amount in litres? Make 5 different 2 digit numbers e.g. 56, 74, 31, 65, 83. Multiply them each by 101. What do you notice? What happens when you multiply each one by 1001?

ThHTU ÷ U divide numbers up to four digits by a 1-digit number using the formal written method of short division and interpret remainder s appropriat ely for the context	Follow processes shown in Year 4 HTU ÷ U with place value counters	240 + 6 <u>8786</u> 1 Chunking on a number li Children should use the key help them with related facts 10 x 7 = 70 100 x 7 = 700 1256 $\div$ 7 = - 490 - 63 - 63 - 63 - 556 Answer: 179 remainder 3 o	facts box to Key Facts 1 x 7 = 7 2 x 7 = 14 5 x 7 = 35 10 x 7 = 70 - Too 12 56	Short division 432 ÷ 5 becomes $8 6 r^2$ $5 4 3^2$ Showing remainder as a whole number: $8 5 8 r^2$ $3 2^2 5^1 7^2 6$ Answer: 858 remainder 2 Showing remainder as a fraction: $8 5 8 r^2$ $3 2^2 5^1 7^2 6$ Answer: 858 $r^2$ $3 2^2 5^1 7^2 6$ Answer: 858 $r^2$ $3 2^2 5^1 7^2 6$	<ul> <li>6 people won £8724 on the lottery. They spent £650 on a party to celebrate then shared the rest. How much did they each receive?</li> <li>How many divisions can you create which leave a remainder of 4/5, 2/3etc.?</li> <li>Try this with several numbers: choose a prime number greater than 3, square it and divide the answer by 12. Look at the remainder. What do you with the several of a function of the several of the several of the several of the several function of the several of the se</li></ul>
s appropriat ely for the		Answer: 179 remainder 3 o		•	numbers: choose a prime number greater than 3, square it and divide the answer by 12. Look at the

Year 6	Concrete	Pictorial	Conceptual	Using and applying
Multiply multi-digit numbers up to 4 digits by a two- digit whole number using the efficient written method of long multiplicati on.	NB: Children should proceed to pictorial methods .	Use grid method for ThHTU xTU (refer to year 5). Grid can also be used to multiply decimal numbers. Use the grid method of multiplication (as below) <u>Grid method</u> $372 \times 24$ is approximately $400 \times 20 = 8000$ Extend to decimals with up to two decimal places. $3.42 \times 6 =$ $\hline{x 3} 0.4 0.02$ 6 18 2.4 0.12 18.0 2.4 0.12 20.52	Compact method 1735 x 43 5205 244 69400 2222 74605 1735 x 43 = 74605	There are 24 bottles in a crate. Each bottle has a capacity of 720ml. what is the total amount in litres? Make 5 different 2 digit numbers e.g. 56, 74, 31, 65, 83. Multiply them each by 101. What do you notice? What happens

Divide	Chunking on a number line.	Short division	There are 432 guests at a
numbers			wedding. Each table at
up to four	Key Facts	quotient	dinner seats 15 people.
digits by a	$2 \times 7 = 14$	divisor 5 847 dividend	How many tables are
2-digit	5 x 7 = 35	divisor 3  04/ dividend	needed?
whole	10 x 7 = 70		
number			A farmer had 450 eggs. 18
using the	Children should use the key facts box to	496 ÷ 11 becomes	smashed so he put the rest
formal	help them with related facts.	45 r 1	into boxes of 15. How
written		5	many boxes did he use?
method of	10 x 7 = 70	1 1 4 9 6	
long	100 x 7 = 700		How many divisions can
division,		Answer: 45 11	you create which result in
and	1256 ÷ 7 =	Both methods above are necessary	a recurring decimal? Can
interpret		at this stage, to deal with the wide range of problems experienced at	you find a pattern in the
remainder	-490 -700	Stage Six.	numbers you used?
s as whole	-63 -700	432 ÷ 15 becomes	Ş
number	Toproups (100 groups)	452 ÷ 15 becomes	Choose a 4 digit number
remainder	(Charles Co. 1	2 8	and investigate fractional
S,	3 66 2556 1256	1 5 4 3 2	and decimal remainders
fractions,		<b>3 0 0</b> 15×20	when you divide by 9.
or by	Answer: 179 remainder 3 or 179 3	1 3 2	What patterns do you
rounding,	7	<b>1 2 0</b> <sup>15×8</sup>	notice?
as		1 2	
appropriat			
e for the		$\frac{12}{15} = \frac{4}{5}$	
context			
		Answer: 28 $\frac{4}{5}$	