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# Fractions, decimals and percentages Calculation Policy

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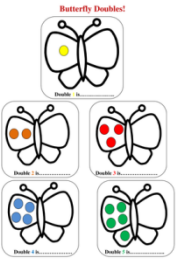

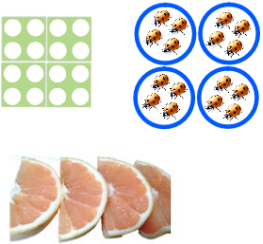
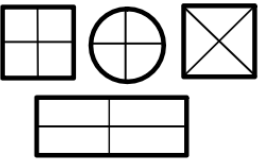
Highlands Primary School

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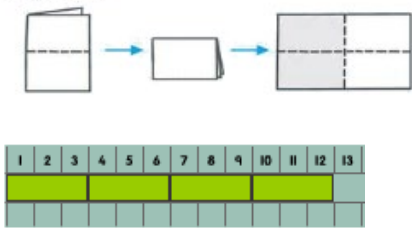
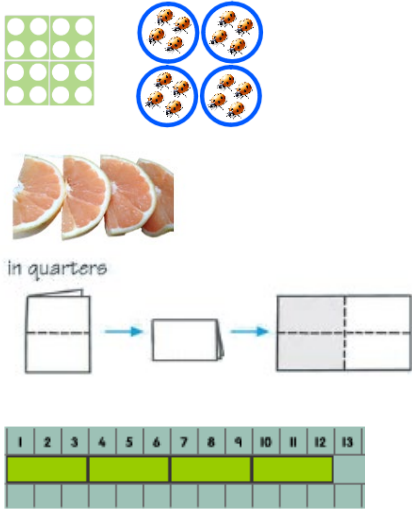
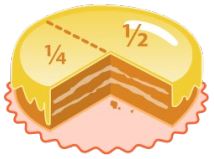
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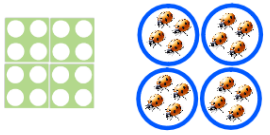
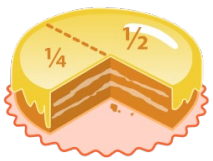
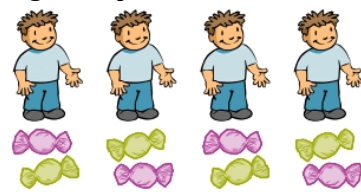
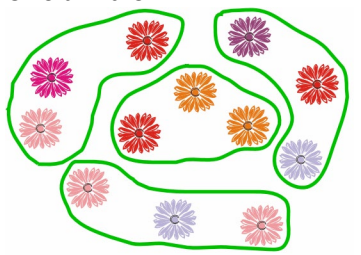
# Fractions, decimals and percentages

EYFS	Concrete	Pictorial	Conceptual	Using and applying
<p>Solves problems, including doubling, halving and sharing (ELG). (Numbers)</p>	<p>Using objects to show double.</p>  <p>Using objects to show half and to share.</p> 	<p>Drawing pictures to show double and to half or 'share'.</p> 	<p>Can I have half of your apple?</p> 	<p>Discussions about sharing objects or halving fruit.</p> <p>If Megan has 3 toys and Maheen has 3 toys, how many toys do they have altogether?</p>
Year 1	Concrete	Pictorial	Conceptual	Using and applying
<p>Recognise, find and name a half as one of two equal parts of an object, shape or quantity</p> <p>Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity</p>	<p>Using familiar objects and resources.</p> <p>Sharing quantities into equal groups.</p> 	<p>Using a variety of models and images</p> 	<p>Recognise unit fraction notation:</p> <p><math>\frac{1}{2}</math> and <math>\frac{1}{4}</math></p>	<p>I had 8 balloons.</p> <p>I gave <math>\frac{1}{4}</math> of them away.</p> <p>How many balloons did I give away?</p> <p>How many do I have left?</p> <p>Use the numbers 1 to 20.</p> <p>Which numbers can you find <math>\frac{1}{2}</math> / <math>\frac{1}{4}</math> of?</p> <p>What do you notice about your answers?</p>

# Fractions, decimals and percentages

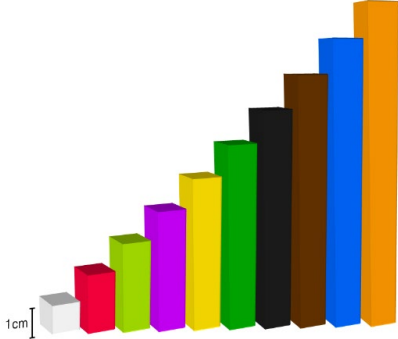
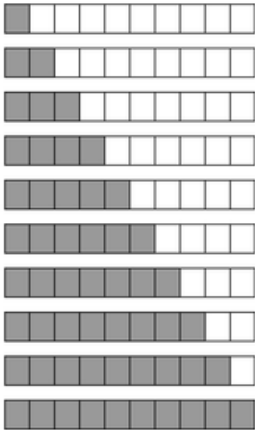
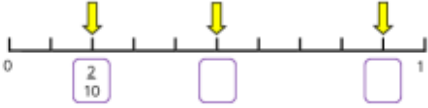
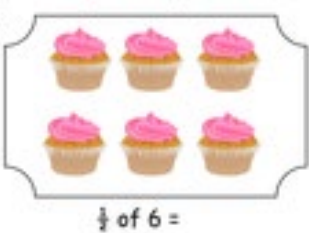
	<p>in quarters</p> 			<p><b>Possible misconceptions</b></p> <ul style="list-style-type: none"> <li>-Children may think that all parts do not need to be equal.</li> <li>- Children may think the bigger the denominator the bigger the part.</li> </ul>
<p><b>Year 2</b></p>	<p><b>Concrete</b></p>	<p><b>Pictorial</b></p>	<p><b>Conceptual</b></p>	<p><b>Using and applying</b></p>
<p>Recognise, find, name and write fractions one third , one quarter , 2 quarters and three quarters of a length, shape, set of objects or quantity.</p>	<p>Using familiar objects and resources. Sharing quantities into equal groups.</p> 	<p>Using a variety of models and images</p> 	<p>Recognise unit and non-unit fraction notation:</p> <p><math>\frac{1}{2}</math> and <math>\frac{1}{4}</math> 2 quarters, three quarters</p>	<p>I had 20 balloons. I gave one two quarters of them away. How many balloons did I give away? How many do I have left?</p> <p><math>\frac{2}{4}</math> is the same as ...? What other fractions are equivalent to <math>\frac{2}{4}</math>?</p>

# Fractions, decimals and percentages

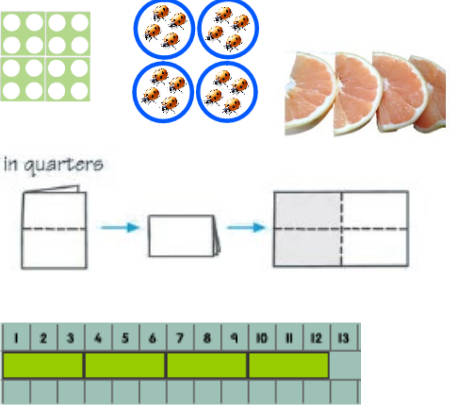
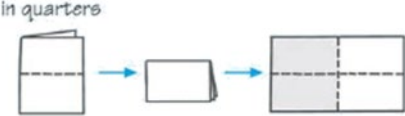
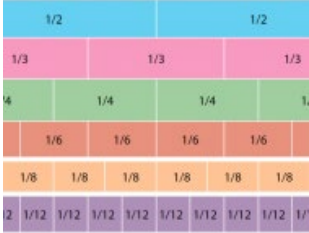
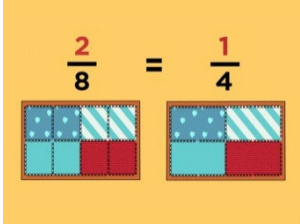
<p>Write simple fractions for example, half of 6 = 3 and recognise the equivalence of 2 quarters and one half.</p>	<p>Using familiar objects and resources. Sharing quantities into equal groups.</p> 	 <p>Sharing and grouping. E.g. one quarter of 8</p>  <p>One third of 12</p> 	<p>Find fractions of quantities:</p> <p><math>\frac{1}{2}</math> of 20  <math>\frac{1}{3}</math> of 18          2 quarters of 24</p>	<p><math>\frac{2}{4}</math> is the same as ...?          What other fractions are equivalent to <math>\frac{2}{4}</math>?</p> <p>Jacob had 24 sweets. He gave one third to his mum, one third to his dad and he kept one third for himself. How many did they have each?</p> <p>Alice, Adam and Maheen have <math>\frac{3}{4}</math> of a cake. How much of the cake is left?</p> <p><b>Possible misconceptions</b></p> <ul style="list-style-type: none"> <li>- Children may think that all parts do not need to be equal.</li> <li>- Children may think the bigger the denominator the bigger the part.</li> <li>- Children may read fractions incorrectly e.g. thinking that <math>\frac{1}{4}</math> is one part shaded, 4 parts not</li> </ul>
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# Fractions, decimals and percentages

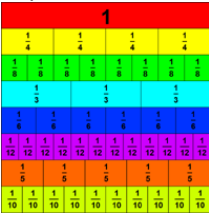
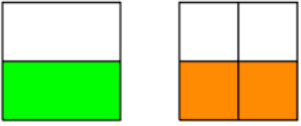
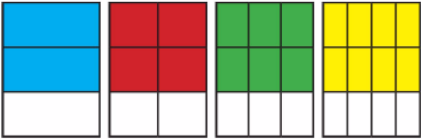
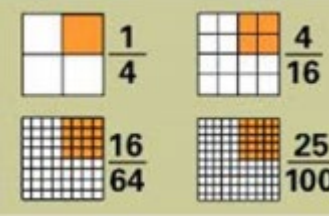
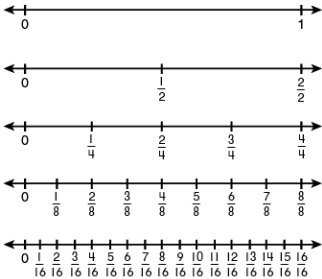
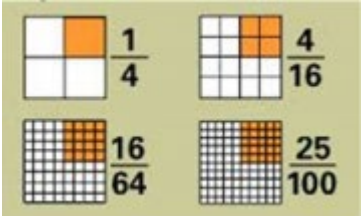
## Lower Key Stage 2:

Year 3	Concrete	Pictorial	Conceptual	Using & applying
<p>Count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10</p>	<p>Using practical resources and objects.</p> 	<p>Structured visual images</p>  <p>Use of number lines</p>	<p>Continue the pattern: 0, 1/10, 2/10, 3/10.....</p>	 <p><b>Possible misconceptions</b>  <i>-Children may not realise it is the denominator which stays the same and the numerator changes.                      -Children may not realise that 10 parts make a whole.</i></p>
<p>Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators</p>	<p>Using familiar objects and resources. Sharing quantities into equal groups.</p>	 <p>Drawing arrays to support finding fractions of objects and numbers.</p>	<p><math>\frac{1}{4}</math> of 24 is 6                      one fifth of 30 is 6                      two fifths of 30 is 12                      three quarters of 28</p>	<p>Ms Davies has a packet of 32 stickers. She uses three quarters of the pack at lunchtime. How many stickers does she have left?</p> <p>I have 7 sweets left. I have eaten <math>\frac{1}{4}</math> of the total bag. How many sweets did I have in the beginning?</p>

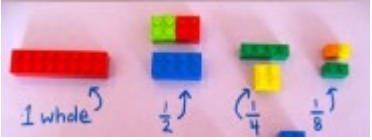
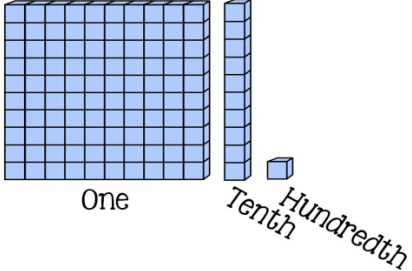
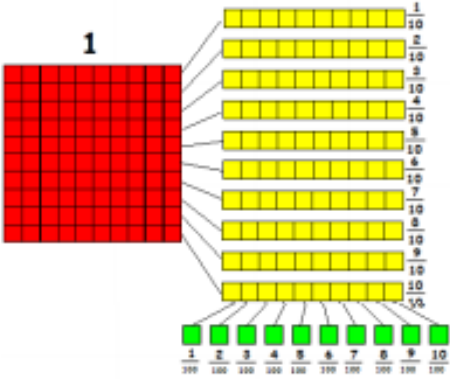
# Fractions, decimals and percentages

<p>Recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators</p>				
<p>Recognise and show, using diagrams, equivalent fractions with small denominators</p>	<p>Use physical objects and resources to recognise equivalence.</p> 	<p>Equivalence on a bar model</p>  	<p>Two quarters is the same as...?</p>	<p>Hassan had five eighths of a pizza. Dylan had one half of a pizza. Who had the most pizza?</p>

# Fractions, decimals and percentages

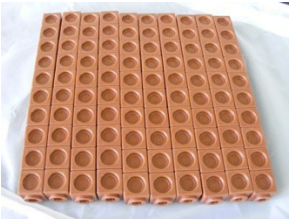
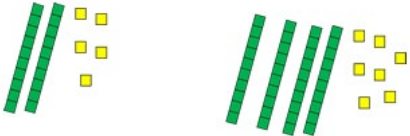
Year 4	Concrete	Pictorial	Conceptual	Using and applying
<p>Recognise and show, using diagrams, families of common equivalent fractions</p>	<p>Explore fraction walls.</p>  <p>Find different fractions of the same thing (e.g. a square or rectangle (on squared paper for ease) or a strip of paper).</p> <p>Match the pieces that are the same size (children can cut out pieces)</p>  <p style="text-align: center;"><math>\frac{1}{2}</math>                      <math>\frac{2}{4}</math></p>  <p style="text-align: center;"><math>\frac{2}{3} = \frac{4}{6} = \frac{6}{9} = \frac{8}{12}</math></p> <p>Using lego.</p>	<p>Structured visual images</p>  <p>Use of number line:</p> 	<p>Find different fractions of the same number and compare which fractions give the same answer.</p> <p><math>\frac{1}{4}</math> of 8 = 2  <math>\frac{2}{4}</math> of 8 = 4  <math>\frac{3}{4}</math> of 8 = 6  <math>\frac{1}{2}</math> of 8 = 4</p> <p>Which two match?</p>	<p>Which fractions are equivalent? How do you know? Can you show me that one quarter is equivalent to four sixteenths?</p>  <p>How are these the same?</p> <p>How are they different?</p> <p><b>Possible misconceptions</b></p> <ul style="list-style-type: none"> <li>-Children may not be able to represent fractions pictorially.</li> <li>-Children may think that the larger the denominator, the larger the fraction.</li> <li>-Children may not realise the importance of finding the unit fraction before moving on to find the non-unit fraction.</li> </ul>

# Fractions, decimals and percentages

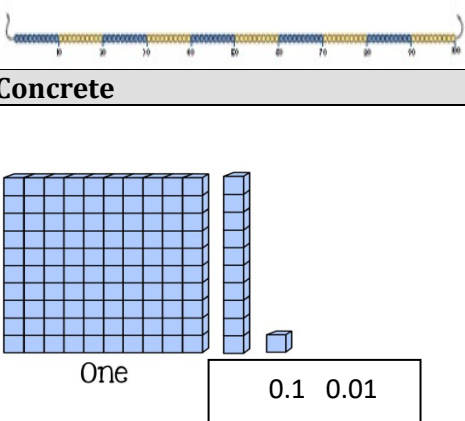
				<p>-Children struggle to use different representations to show a fraction.</p>
<p>Recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten</p>	<p>Use Dienes equipment.</p>  <p>'Blow up' Dienes so: Flat = 1, Long = 1/10 = 0.1 and Unit = 1/100 = 0.01</p>  <p>What fraction is each piece?          How many hundredths make one 1/10?          How many hundredths make one whole?</p>	<p>Place value chart.</p>	<p> <math>1 \div 100 = 1/100</math>  <math>2 \div 100 = 2/100</math>  <math>3 \div 10 = 3/10</math>  <math>27 \div 100 = 27/100</math> </p>	<p><b>What do you notice?</b></p> <p> <math>1/10</math> of 100 = 10  <math>1/100</math> of 100 = 1  <math>2/10</math> of 100 = 20  <math>2/100</math> of 100 = 2         </p> <p>How can you use this to work out  <math>6/10</math> of 200?  <math>6/100</math> of 200?</p> <p><b>Possible misconceptions</b></p> <p>-Children may think that the larger the denominator, the larger the fraction.          -Children may not make the relationship between <math>1/10</math> and <math>10/100</math>.</p>



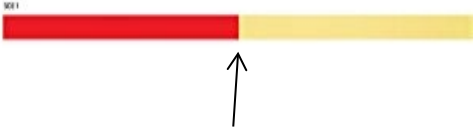
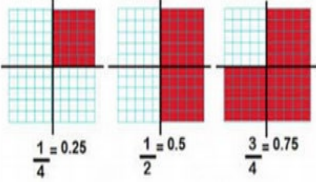


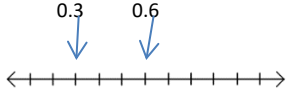
# Fractions, decimals and percentages

	<p>Multilink can also be used where children physically break up the unit.</p> 			
<p>Count up and down in hundredths.</p>	<p>Review counting in tenths before moving onto hundredths.</p> <p>Using the dienes rods, where 1 flat = 1 whole, 1 rod = 1 tenth. 1 unit = 1 hundred – children to physically move a unit piece and count in hundredth.</p> <p>Children to then recognise that 1 rod is the same as 10/100.</p> <p>If the start from 25/100 children to then add 1 unit rod whilst counting in hundredth.</p>  <p>Use beads string to count up in 10<sup>th</sup> and 100ths.</p>	<p>Structured visual images</p> <p>Use of number lines</p>	<p>Continue the pattern: 0, 22/100, 23/100, 24/100, 25/100.....</p> <p>Count in hundredths from zero, then from any whole number, any hundredth and then any number (e.g. 2 and a half, 2 and 51 hundredths...)</p> <p>Which is greatest: one tenth or one hundredth?</p>	<p><b>Spot the mistake</b> sixty tenths, seventy tenths, eighty tenths, ninety tenths, twenty tenths ... and correct it.</p> <p><b>What comes next?</b> 83/100, 82/100, 81/100, ....., ....., .....</p> <p><b>Possible misconceptions</b> -Children may not realise when counting up, denominator stays the same and the numerator changes. -Children may not realise that 100 parts make a whole. Children may not recognise that 1/10 is bigger than 1/100</p>

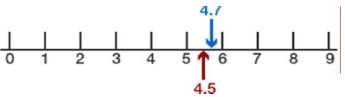
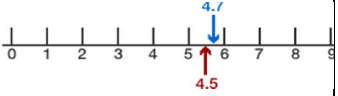
# Fractions, decimals and percentages

Year 4	Concrete	Pictorial	Conceptual	Using and applying												
<p>Recognise and write decimal equivalents of any number of tenths or hundredths.</p>		$\frac{1}{10} \quad \frac{1}{100}$ $0.10 \quad 0.100$ $0.1 = \frac{1}{10}$ $0.2 = \frac{2}{10}$ $0.01 = \frac{1}{100}$		<p><b>Using and applying</b></p> <p>Complete the pattern by filling in the blank cells in this table:</p> <table border="1" data-bbox="1576 405 1890 628"> <tbody> <tr> <td><math>\frac{1}{10}</math></td> <td><math>\frac{2}{10}</math></td> <td><math>\frac{3}{10}</math></td> <td></td> </tr> <tr> <td><math>\frac{10}{100}</math></td> <td><math>\frac{20}{100}</math></td> <td></td> <td><math>\frac{40}{100}</math></td> </tr> <tr> <td>0.1</td> <td></td> <td>0.3</td> <td></td> </tr> </tbody> </table> <p><b>Another and another</b> Write a decimal numbers (to one decimal place) which lies between a half and three quarters? ... and another, ... and another,</p> <p><b>Possible misconceptions</b> <i>Children may not recognise the bigger the denominator the smaller the parts.</i> <i>Children may think that 0.01 is bigger than 0.1.</i></p>	$\frac{1}{10}$	$\frac{2}{10}$	$\frac{3}{10}$		$\frac{10}{100}$	$\frac{20}{100}$		$\frac{40}{100}$	0.1		0.3	
$\frac{1}{10}$	$\frac{2}{10}$	$\frac{3}{10}$														
$\frac{10}{100}$	$\frac{20}{100}$		$\frac{40}{100}$													
0.1		0.3														

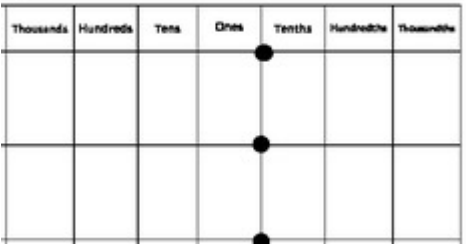
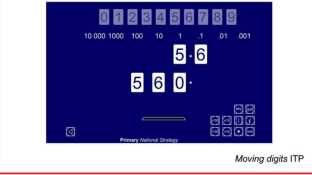
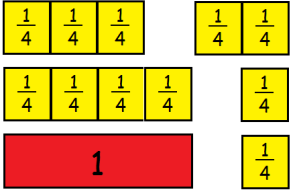




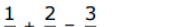
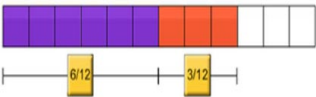
# Fractions, decimals and percentages

<p>Recognise and write decimal equivalents to <math>\frac{1}{4}</math>, <math>\frac{1}{2}</math>, <math>\frac{3}{4}</math></p>	<p>Use a counting stick marked in divisions of 0.5 to familiarise children with counting forwards and backwards in steps of 0.5 (link to counting forwards and backwards in <math>\frac{1}{2}</math>).</p> <p>What fraction does this present?</p> 	<p>Use 10x10 grids and establish each square is one hundredth (0.01). Find fractions of the square (100) and use it to write decimal equivalents.</p> 	<p>Continue the pattern – 0.25, 0.5, 0.75, 1, 1.25, 1.5.....</p> <p>Counting on the counting stick in <math>\frac{1}{4}</math> and 0.25.</p> <p>Missing numbers.</p>	<p><b>Ordering</b></p> <p>Put these numbers in the correct order, starting with the smallest.</p> <p><math>\frac{1}{4}</math> 0.75 5/10</p> <p>Explain your thinking</p> <p><b>Possible misconceptions</b></p> <p>Children <math>\frac{1}{2}</math> is the same as 5/10 which is the same as 0.5.</p> <p>Children may not recognise that 0.25 is half of 0.5.</p>
<p>Compare numbers with the same number of decimal places up to two decimal places.</p>	<p>Help children become aware of the relative size of decimal numbers by ordering a set of amounts of money or lengths.</p> <p>£1.23</p>  <p>£1.03</p> 	<p>Position decimals on a number line for children to get a sense of size.</p> 	<p>Put these numbers in descending order:</p> <p>1.23, 1.03, 1.31, 1.32, 1.02</p> <p>Include numbers to overcome misconceptions such as mistaking the length of the number with its size, for example thinking that 4.05 is larger than 4.5.</p>	<p><b>Missing symbol</b></p> <p>Put the correct symbol &lt; or &gt; in each box</p> <p>3.03 <input type="checkbox"/> 3.33</p> <p>0.37 <input type="checkbox"/> 0.32</p> <p>What needs to be added to 3.23 to give 3.53?</p> <p>What needs to be added to 3.16 to give 3.2?</p> <p>Which is the larger amount, £0.75 or 90p? Which is longer, 3.06 m or 3.6 m? Which is larger: 239p or £2.93? Why?</p> <p><b>Possible misconceptions</b></p>

# Fractions, decimals and percentages

				<p><i>Children may think that 0.09 is bigger than 0.2 because '9' is larger than '2'.</i></p>
<p>Round decimals with one decimal place to the nearest whole number</p>	<p>Present children with a number line and digit cards (whole numbers).</p>  <p>Call out a number – children to hold up the digit cards the number is closest to.</p>	<p>Children to place digits on a number line, draw how many jumps to the whole numbers either side.</p> 	<p>1.7 → 2 2.5 → 3 1.4 → 1 8.2 → 8</p>	<p>What is 4.7 rounded to the nearest whole number? I rounded my number to 3. What number (with one decimal place) could it have been? What is the biggest/smallest number I would round to 2? Simon rounded 1.6 to 2. Was he right? Explain how you know. Show me why I would round 2.3 to 2. My chair is nearly 1 m high. How tall could it be?</p> <p><b>Do, then explain</b> Circle each decimal which when rounded to the nearest whole number is 5. 5.3 5.7 5.2 5.8 Explain your reasoning</p> <p><b>Possible misconception</b> <i>-Children may find the next multiple instead of the closest multiple.</i></p>
<p>Find the effect of dividing</p>	<p>Use place value grids.</p>	<p>ITP</p>	<p>Create numbers and look at effect of dividing by 10 and 100. Explore the visual</p>	<p>What is ... ÷ 10 ÷ 100 ? How do you know? Can you show me? How to divide by ten? What mistake Have I made here?</p>

# Fractions, decimals and percentages

<p>a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths.</p>	<p><b>PLACE VALUE CHART</b></p> 	<p>Use the Moving digits ITP to model the effect of multiplying and dividing by 10, 100 and 1000.</p>  <p>Primary National Strategy Moving digits ITP</p> <p>Demonstrate the effect of dividing a number by 10. Show children how the digits move one place to the right, and when dividing by 100 the digits move two places to the right.</p> <table border="1"> <tr> <td>Th</td> <td>H</td> <td>T</td> <td>U</td> </tr> <tr> <td>2</td> <td>5</td> <td>0</td> <td>0</td> </tr> <tr> <td>2</td> <td>5</td> <td>0</td> <td>0</td> </tr> <tr> <td>3</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>3</td> <td>0</td> <td>0</td> <td>0</td> </tr> </table> <p>This shows that <math>250 \div 10 = 25</math> This shows that <math>3000 \div 100 = 30</math></p>	Th	H	T	U	2	5	0	0	2	5	0	0	3	0	0	0	3	0	0	0	<p>pattern of the digits within division.</p> <table border="1"> <tr> <td><math>400 \div 100 = 4</math></td> <td><math>400 \div 10 = 40</math></td> </tr> <tr> <td><math>40 \div 10 = 4</math></td> <td><math>40 \div 10 = 4</math></td> </tr> <tr> <td><math>4 \div 1 = 4</math></td> <td><math>4 \div 10 = 0.4</math></td> </tr> <tr> <td><math>0.4 \div 0.1 = 4</math></td> <td><math>0.4 \div 10 = 0.04</math></td> </tr> </table>	$400 \div 100 = 4$	$400 \div 10 = 40$	$40 \div 10 = 4$	$40 \div 10 = 4$	$4 \div 1 = 4$	$4 \div 10 = 0.4$	$0.4 \div 0.1 = 4$	$0.4 \div 10 = 0.04$	<p><b>Possible misconceptions</b></p> <ul style="list-style-type: none"> <li>-Children may not be secure with what way to move the digits on the place value chart.</li> <li>-When dividing or multiplying a number with a 0 in between other digits i.e. 403, children may remove the 0.</li> </ul>
Th	H	T	U																													
2	5	0	0																													
2	5	0	0																													
3	0	0	0																													
3	0	0	0																													
$400 \div 100 = 4$	$400 \div 10 = 40$																															
$40 \div 10 = 4$	$40 \div 10 = 4$																															
$4 \div 1 = 4$	$4 \div 10 = 0.4$																															
$0.4 \div 0.1 = 4$	$0.4 \div 10 = 0.04$																															
<p>Add and subtract fractions with the same denominator</p>	<p>Use fraction cards to model the process.</p>  <p>Using lego:</p>  <p>Numicon</p> $\frac{2}{9} + \frac{6}{9} = \frac{8}{9}$	<p><math>\frac{1}{5} + \frac{2}{5} = \frac{3}{5}</math></p>  <p><math>\frac{1}{5}</math></p>  <p><math>\frac{2}{5}</math></p>  <p><math>\frac{3}{5}</math></p>  <p><math>\frac{1}{5} + \frac{2}{5} = \frac{3}{5}</math></p> <p><math>\frac{6}{12} + \frac{3}{12} = \frac{9}{12}</math></p> 	<p><math>\frac{1}{5} + \frac{2}{5} = \frac{3}{5}</math></p> <p><math>\frac{6}{12} + \frac{3}{12} = \frac{9}{12}</math></p>	<p><b>What do you notice?</b></p> <p><math>\frac{5}{5} - \frac{1}{5} = \frac{4}{5}</math></p> <p><math>\frac{4}{5} - \frac{1}{5} = \frac{3}{5}</math></p> <p><b>Continue the pattern</b></p> <p><b>Possible misconceptions</b></p> <ul style="list-style-type: none"> <li>-Children may not be secure in understanding why the denominators doesn't change resulting in them adding or subtracting them.</li> </ul>																												

# Fractions, decimals and percentages

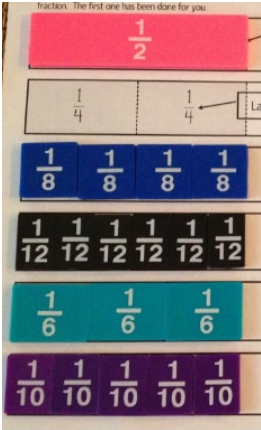
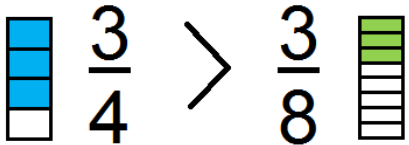
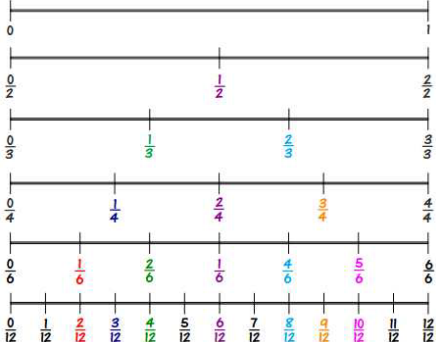


$$\frac{6}{6} - \frac{2}{6} = \frac{4}{6}$$

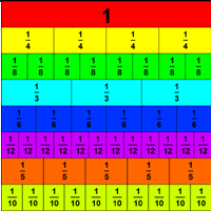
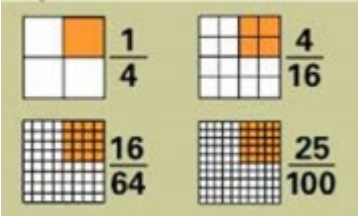


# Fractions, decimals and percentages

## Upper Key Stage 2:

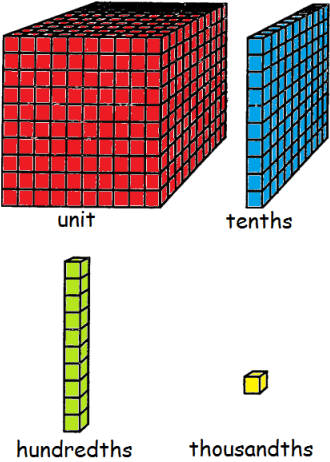
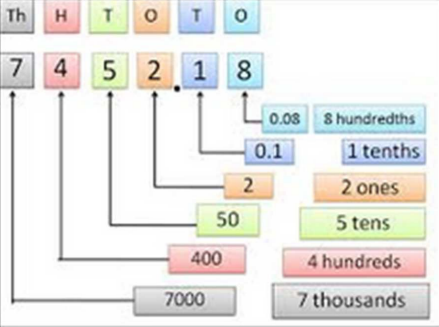

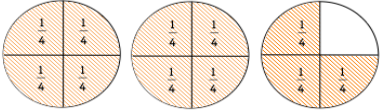
Year 5	Concrete	Pictorial	Conceptual	Using and applying
<p>Compare and order fractions with denominators that all have multiples of the same number.</p>	<p>Use fraction cards or a fraction wall to physically compare the sizes of fractions.</p>  <p>Make links between the fraction sign and division.</p> <p>Use a calculator to perform the division and compare the decimal numbers, then relate them to the original fraction.</p>	<p>Draw objects which are the same size to compare.</p>  <p>Use of number line to compare fractions.</p> 	<p>Use knowledge of simplifying and finding a common denominator to compare fractions with denominators that all have multiples of the same number.</p>	<p>Give an example of a fraction that is more than three quarters.</p> <p>Now another example that no one else will think of. Explain how you know the fraction is more than three quarters.</p> <p><b>Possible misconceptions</b> -Children may not be secure in finding equivalent fractions.</p> <p>Children may not find the lowest common denominator resulting in them working in efficiently.</p>
<p>Identify, name and write</p>	<p>Use various models and images to represent fractions in different ways.</p>	<p>Use of fraction wall to find equivalence</p>	<p>Investigate using multiplication and division to create equivalent fractions and to</p>	<p><b>Odd one out.</b> Which is the odd one out in each of these collections of 4 fractions:</p>

# Fractions, decimals and percentages

<p>equivalent fractions of a given fraction, represented visually, including tenths and hundredths</p>		 	<p>simplify fractions to find simplest equivalent.</p>	$\frac{6}{10} \quad \frac{3}{5} \quad \frac{18}{20} \quad \frac{9}{15}$ $\frac{30}{100} \quad \frac{3}{10} \quad \frac{6}{20} \quad \frac{3}{9}$ <p>Why?</p> <p><b>Possible misconceptions</b>  <i>-Although children may be able to find equivalent fractions, they may not fully understand they represent the same the size of a given value – lots of practical example will support their understanding of equivalent fractions.</i>  <i>-Children may struggle to recognise common multiples.</i>  <i>-Children may struggle to visualise when two fractions are equivalent.</i></p>
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# Fractions, decimals and percentages

Year 5	Concrete	Pictorial	Conceptual	Using and applying
<p>Recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents.</p>	<p>Blow up' dienes so 1 cube represents 1 whole, and therefore unit cubes represent one thousandths.</p> 		<p>Symbols: <math>1 + 10, 1 + 100, 1 + 1000</math></p> $\frac{1}{10} \frac{1}{100} \frac{1}{1000}$ <p>3.652 = 'three point six five = three units, six tenths, 5 hundredths and 2 thousandths = 3652 thousandths</p>	<p>How would you read this number 1.234? What is the place value of each digit? How many units are there? How many tenths? How many hundredths? How many thousandths?</p> <p><b>Possible misconceptions</b> -Children may not recognise that <math>1/100</math> is bigger than <math>1/1000</math>. -Children may not make the relationship between <math>1/100</math> and <math>10/1000</math>. -Children may think that <math>0.001</math> is bigger than <math>0.1</math> because it has more digits.</p>
<p>Recognise mixed numbers and improper fractions and convert from one form to the other.</p>	<p>1 or <math>\frac{1}{4}</math> <math>1 \frac{1}{4}</math> or <math>\frac{5}{4}</math> <math>1 \frac{1}{2}</math> or <math>\frac{3}{2}</math></p> 	<p>How many quarters are there in 2 and <math>\frac{3}{4}</math>?</p>  <p><math>2 \frac{1}{2} = 7</math></p>	<p><math>\frac{7}{3} = 2 \frac{1}{3}</math></p> <p>How many groups of 3 are there in 7? What is the remainder? Or <math>7 \div 3 = 2 \text{ r } 1</math></p>	<p>Tell me a fraction that is bigger than 3. How else could we write it?</p> <p>Show me what eight thirds looks like. What is equivalent to it? How can you prove it?</p>

# Fractions, decimals and percentages

How many quarters make a whole?

Use knowledge of counting to mark numbers on number lines.



Numicon stack



With the whole as ten, each peg represents  $1/10$ . Children can then stack up the numicon to show any improper fractions. For example, the picture above shows  $1 \frac{3}{10}$  or  $13/10$

3 3



3

## **Possible**

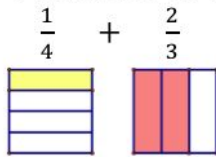
### **misconceptions**

- Children may not consider that a fraction can be larger than a whole.
- Children may think that mixed numbers are larger than improper fractions.

# Fractions, decimals and percentages

Add and subtract fractions with the same denominator and denominators that are multiples of the same number and write mathematical statements > 1 as a mixed number [e.g.  $\frac{3}{5} + \frac{4}{5} = \frac{6}{5} = 1 \frac{1}{5}$ ]

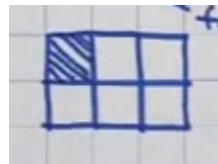
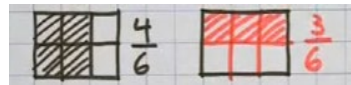
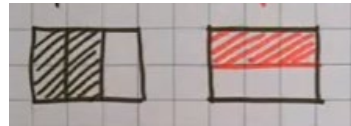
## ADDING FRACTIONS



$$\frac{3}{12} + \frac{8}{12} = \frac{11}{12}$$

## Subtracting fractions

$$\frac{2}{3} - \frac{1}{2} =$$



Answer =  $\frac{1}{6}$

$$\frac{1}{3} + \frac{1}{5}$$

$$\frac{1}{3} \times 5 = \frac{5}{15} + \frac{1}{5} \times 3 = \frac{3}{15}$$

$$\frac{5}{15} + \frac{3}{15} = \frac{8}{15}$$

## What do you notice?

$$\frac{3}{4} \text{ and } \frac{1}{4} = \frac{4}{4} = 1$$

$$\frac{4}{4} \text{ and } \frac{1}{4} = \frac{5}{4} = 1 \frac{1}{4}$$

$$\frac{5}{4} \text{ and } \frac{1}{4} = \frac{6}{4} = 1 \frac{2}{4}$$

Continue the pattern up to the total of 2.

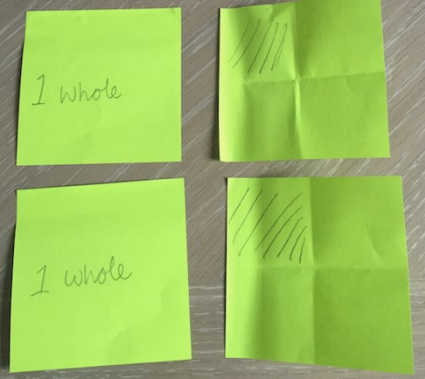
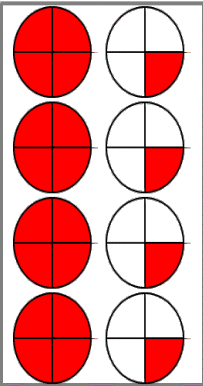
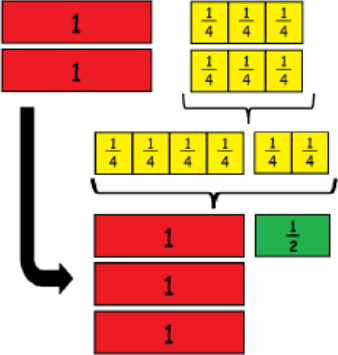
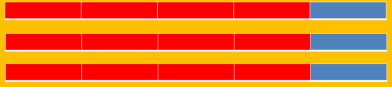
Can you make up a similar pattern for subtraction?

## Possible misconceptions

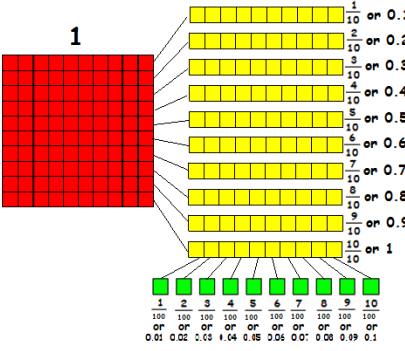

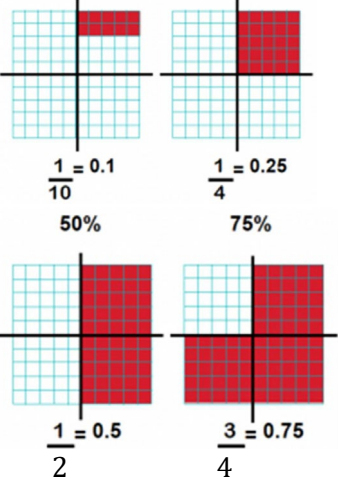
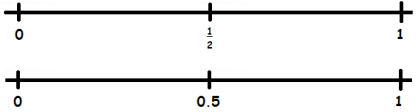
-Children may add the denominators and numerators.

-Children may not use the lowest common multiple to convert the denominator.


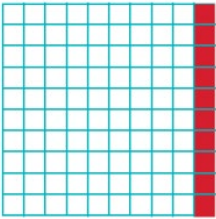
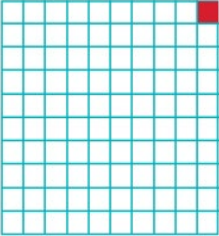


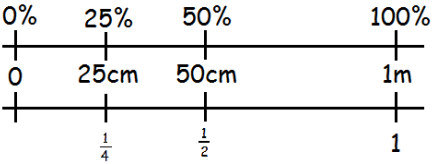
# Fractions, decimals and percentages

Year 5	Concrete	Pictorial	Conceptual	Using and applying
<p>Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams.</p>	<p>Use post it notes to multiply</p> $1 \frac{1}{4} \times 2 =$ 	 <p>4 wholes and 4 quarters = 5</p> $1 \frac{1}{4} \times 4 =$ <p>Images: <math>1 \frac{1}{4} \times 2</math></p>  <div style="background-color: yellow; padding: 5px; text-align: center;"> <math>3 \times 4 = 5</math>  </div>	<div style="border: 1px solid black; padding: 5px; margin-bottom: 10px;"> <math display="block">1 \frac{1}{4} \times 4 =</math> </div> <div style="border: 1px solid black; padding: 5px;"> <math display="block">\frac{5}{4} \times \frac{4}{1} = \frac{20}{4} = 5</math> </div>	<p><b>Continue the pattern</b></p> $\frac{1}{4} \times 3 =$ $\frac{1}{4} \times 4 =$ $\frac{1}{4} \times 5 =$ <p>Continue the pattern for five more number sentences. How many steps will it take to get to 3?</p>

# Fractions, decimals and percentages

		$\frac{12}{5} = 2 \frac{2}{5}$		
<p>Read and write decimal numbers as fractions [for example, 0.71 = 71/100]</p>	<p>Use Dienes to represent decimal numbers and compare to Dienes as fractions.</p>  <p>Numicon</p>  <p>With the whole as ten, each peg represents 1/10 (0.1). Children can then stack up the numicon to show any decimal number. For example the picture above shows 1.3 or 1 3/10 or 13/10.</p>	 <p>Number line</p> 	<p><math>\frac{71}{100} = 71 \div 100</math></p> <p>100</p> <p>Use place value chart to show this represents 0.71.</p>	<p><b>Odd one out.</b> Which is the odd one out in each of these collections of 4 fractions 6/10 3/5 18/20 9/15 30/100 3/10 6/20 3/9 Why? <b>What do you notice?</b> Find 30/100 of 200 Find 3/10 of 200 What do you notice? Can you write any other similar statements?</p> <p><b>Possible misconceptions</b> -Children may not recognise that 1/100 is bigger than 1/1000. -Children may not make the relationship between 1/10 and 10/1000. -Children may think that 0.01 is bigger than 0.1 because it has more digits. Children may not make the link between place value and fractions.</p>

# Fractions, decimals and percentages

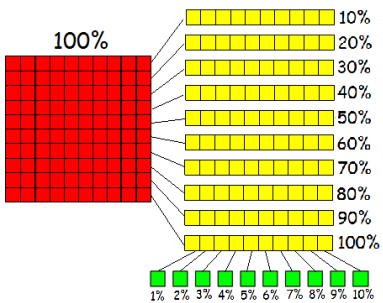
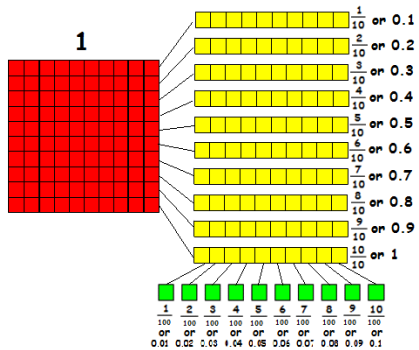
<p>Recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred', and write percentages as a fraction with denominator 100, and as a decimal.</p>	<p>Using the bead bar. Use the bead bar to discuss how many 10% we can get out of 100%.</p> <p>How many parts out of the 10 does 10%/20%/30% represent?</p>  <p>How can we write that as a fraction?</p> <p>Using money. Use money to show how 10p can be expressed as a percentage and a fraction of £1. Give children the opportunity to use coins to convince themselves that, for example, 10p is 1/10 or 10% of £1 because they need ten 10p coins to make £1.</p>	<p>Represent percentage pictorially on a 100 square.</p>  <p><math>10\% = \frac{1}{10} = 0.1</math></p>  <p><math>1\% = \frac{1}{100} = 0.01</math></p> <p>Images of everyday objects:</p>  <p><math>\frac{1}{2} = 50\% = 0.5</math></p>	<p>Percentage is a fraction out of 100.</p> <p><math>1\% = \frac{1}{100} = 0.01</math></p> <p><math>70\% = \frac{70}{100} = 0.7</math></p>	<p>How can you model a percentage?</p> <p><b>Ordering</b> Put these numbers in the correct order, starting with the largest. 7/10, 0.73, 7/100, 0.073, 71%</p> <p>Explain your thinking</p> <p>Which is more: 20% of 200 or 25% of 180? Explain your reasoning.</p> <p><b>Possible misconceptions</b> -Children may not make the link between fractions percentages. -Children may not be able to find equivalent fractions to make the denominator out of 100.</p>
<p>Understand and use the equivalence between percentages, fractions</p>	<p>Counting stick to see the equivalence between the numbers.</p> 	<p>Using a number line</p> 	<p>Use equivalence to represent fraction as part of 100. Use place value chart to show how <math>25 \div 100 = 0.25</math></p> <p><math>\frac{1}{4} = \frac{25}{100} = 25\% = 0.25</math></p>	<p>Fill in the missing numbers in the Grid</p>

# Fractions, decimals and percentages

and decimals (e.g. 100% is a whole quantity and 1% is  $1/100$ , 50% of 100 is 50) and relate this to finding 'fractions of' to solve problems.

Find 50% of a metre. How many cm is this?  
How could this be written as a fraction?

Use dienes to represent whole as 1 or 100%



4 100

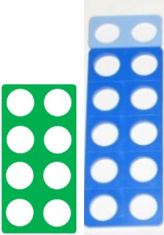
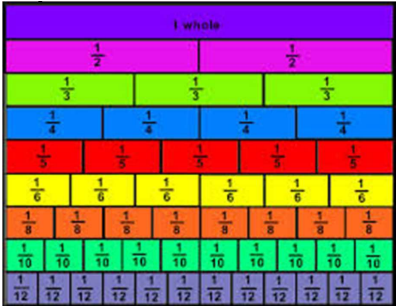
Fraction:  $\frac{\quad}{100}$

Decimal:  $\quad$

Percent:  $\quad\%$

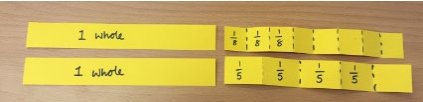


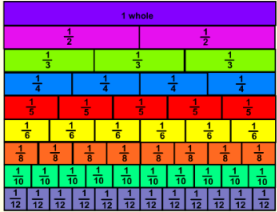
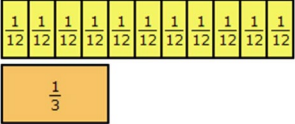
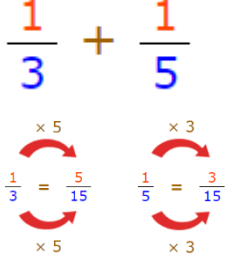
How do you know that 50% is the same as a half?  
How can you show me?

# Fractions, decimals and percentages

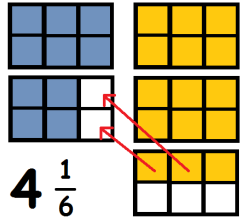
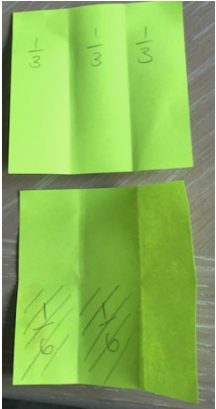
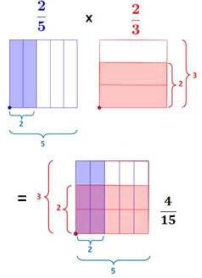
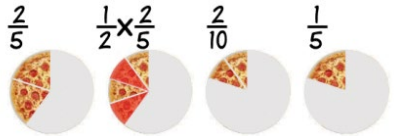
Year 6	Concrete	Pictorial	Conceptual	Using and applying
<p>Use common factors to simplify fractions; use common multiples to express fractions in the same denomination</p>	<p>Numicon to find common factors.</p> $\frac{8}{12} = \frac{2}{3}$ 	<p>Use fraction wall to show equivalence of:</p> $\frac{8}{12} = \frac{2}{3}$ 	<p>Model dividing numerator and denominator by the same number:</p> $\frac{8}{12} (\div 4) = \frac{2}{3}$	<p>What is the missing number?</p> $\frac{7}{10} = \frac{\square}{30}$ <p>How do you know? Tell me a fraction that is equivalent to <math>\frac{1}{2}</math> but has a denominator of 9. How did you do it?</p> <p>Find the missing number:</p> $\frac{3}{\square} = \frac{12}{16}$ <p>Karen makes a fraction using two number cards.</p> <p>She says, 'My fraction is equivalent to <math>\frac{1}{2}</math>. One of the number cards is 6'</p> <p><b>Possible misconceptions</b> -Children may not recognise the lowest common denominator.</p>



# Fractions, decimals and percentages

<p>Compare and order fractions, including fractions <math>&gt; 1</math></p>	<p>Using strips of paper:</p> <p>Which is greater <math>2\frac{4}{5}</math> or <math>2\frac{3}{8}</math> ?</p>  <p>Which is greater <math>\frac{5}{4}</math> or <math>1\frac{1}{2}</math> ?</p> 	<p>Which is greater?</p> $\frac{5}{4} \qquad 1\frac{1}{2}$ 	<p>Find a common denominator:</p> $\frac{5}{4} \qquad 1\frac{1}{2} = 1\frac{2}{4}$ <p>Convert both into a mixed number or improper fraction.</p>	<p>Give an example of a <b>fraction</b> that is greater than 1.1 and less than 1.5. Now another example that no one will think of. Explain how you know.</p> <p><b>Possible misconceptions</b></p> <ul style="list-style-type: none"> <li>-Children may not recognise that fraction can be more than one whole.</li> <li>-Children may think the larger the denominator, the larger the part.</li> <li>-Children may not recognise the lowest common denominator.</li> </ul>
<p>Add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions</p>	<p>Use fraction wall cards :</p> $\frac{11}{12} - \frac{1}{3} =$ 	<p>Bar modelling:</p> $\frac{11}{12} - \frac{1}{3} = ?$  <p>Find a common denominator:</p>	$\frac{1}{3} + \frac{1}{5}$  $\frac{5}{15} + \frac{3}{15} = \frac{8}{15}$	<p>Of the flags in Jackie's Flag Shop, <math>\frac{3}{5}</math> are green and another <math>\frac{1}{5}</math> are teal. What fraction of the flags are either green or teal?</p> <p>Sadie's milkshake recipe needs <math>\frac{3}{4}</math> of a scoop of ice cream and Robbie's recipe needs for <math>\frac{1}{4}</math> of a scoop.</p>

# Fractions, decimals and percentages

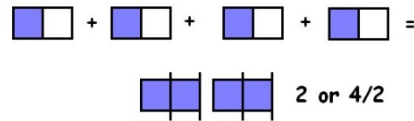
		<p><math>1\frac{2}{3} + 2\frac{1}{2}</math></p> <p>Use denominators to draw grids (in this case <math>2 \times 3</math>) that represent units.</p>  <p><math>4\frac{1}{6}</math></p>		<p>How many more scoops of ice cream are used in Sadie's recipe than in Robbie's recipe?</p>
<p>Multiply simple pairs of proper fractions, writing the answer in its simplest form.</p>	<p>Use post it notes (or cut up paper grids) to model the process of multiplying fractions.</p> <p><math>\frac{2}{3} \times \frac{1}{2} = \frac{2}{6}</math></p> 	<p>Draw grids to multiply, emphasise use of 'of' in place of x.</p>  <p><math>\frac{1}{2} \times \frac{2}{5} =</math></p> 	<p><math>\frac{1}{2} \times \frac{2}{5} = \frac{1 \times 2}{2 \times 5} = \frac{2}{10}</math></p>	<p>The answer is <math>\frac{1}{8}</math>, what is the question (involving fractions / operations)</p> <p><b>Possible misconceptions</b> -children may learn rule and not understand what the mathematics looks like.</p>

# Fractions, decimals and percentages

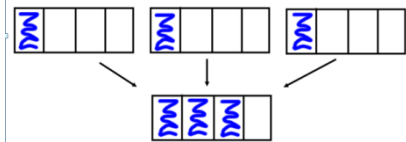
Fraction multiplied by a whole number:

Link multiplication to repeated addition.

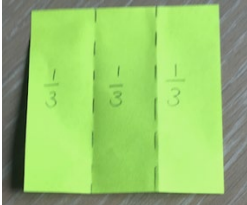
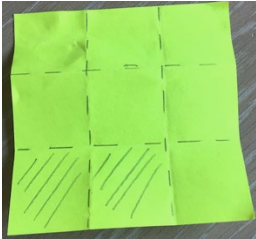
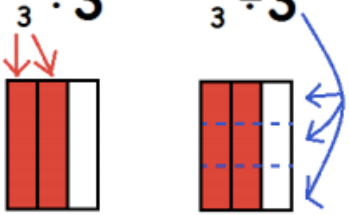
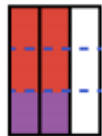
$$4 \times \frac{1}{2} \text{ or } \frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2}$$



$$\frac{1}{4} \times 3 = \frac{3}{4}$$



# Fractions, decimals and percentages

<p>Divide proper fractions by whole numbers</p>	<p>Use post it notes (or cut up paper grids) to model the process of dividing fractions.</p> <p><math>\frac{2}{3} \div 3 = \frac{2}{9}</math></p>  	<p><math>\frac{2}{3} \div 3</math>      <math>\frac{2}{3} \div 3</math></p>  <p><math>\frac{2}{3} \div 3 = \frac{2}{9}</math></p> 	<p><math>\frac{2}{3} \div 3 =</math></p> <p>Discuss that dividing by 3 is the same as multiplying by <math>\frac{1}{3}</math>.</p> <p><math>\frac{2}{3} \div 3 = \frac{2}{3} \times \frac{1}{3}</math></p> <p><math>\frac{2}{3} \times \frac{1}{3} = \frac{2}{9}</math></p>	<p><b>Continue the pattern</b></p> <p><math>\frac{1}{3} \div 2 = \frac{1}{6}</math></p> <p><math>\frac{1}{6} \div 2 = \frac{1}{12}</math></p> <p><math>\frac{1}{12} \div 2 = \frac{1}{24}</math></p> <p><b>Possible misconceptions</b>          -children may learn rule and not understand what the mathematics looks like.</p>
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